

Spatio-temporal modelling of visceral leishmaniasis (VL) among domestic dogs in rural Brazil



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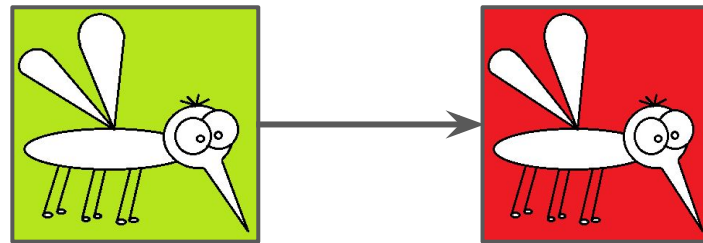


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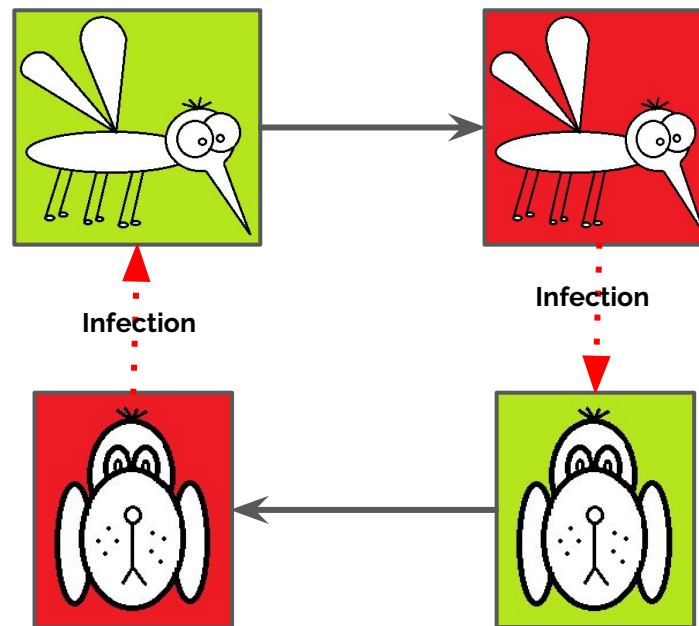
Zoonotic VL

- A vector-borne disease spread by **sandflies**.



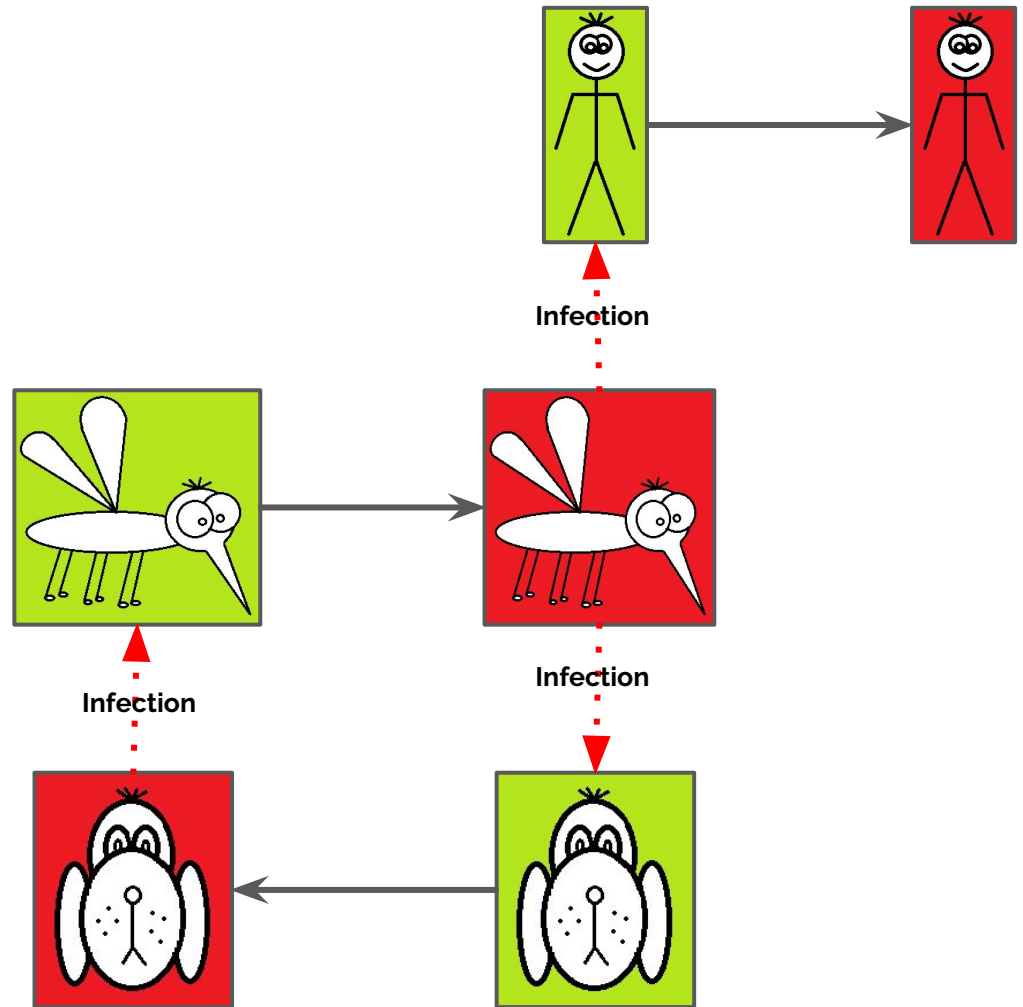
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- In Brazil, **domestic dogs** are the main reservoir.



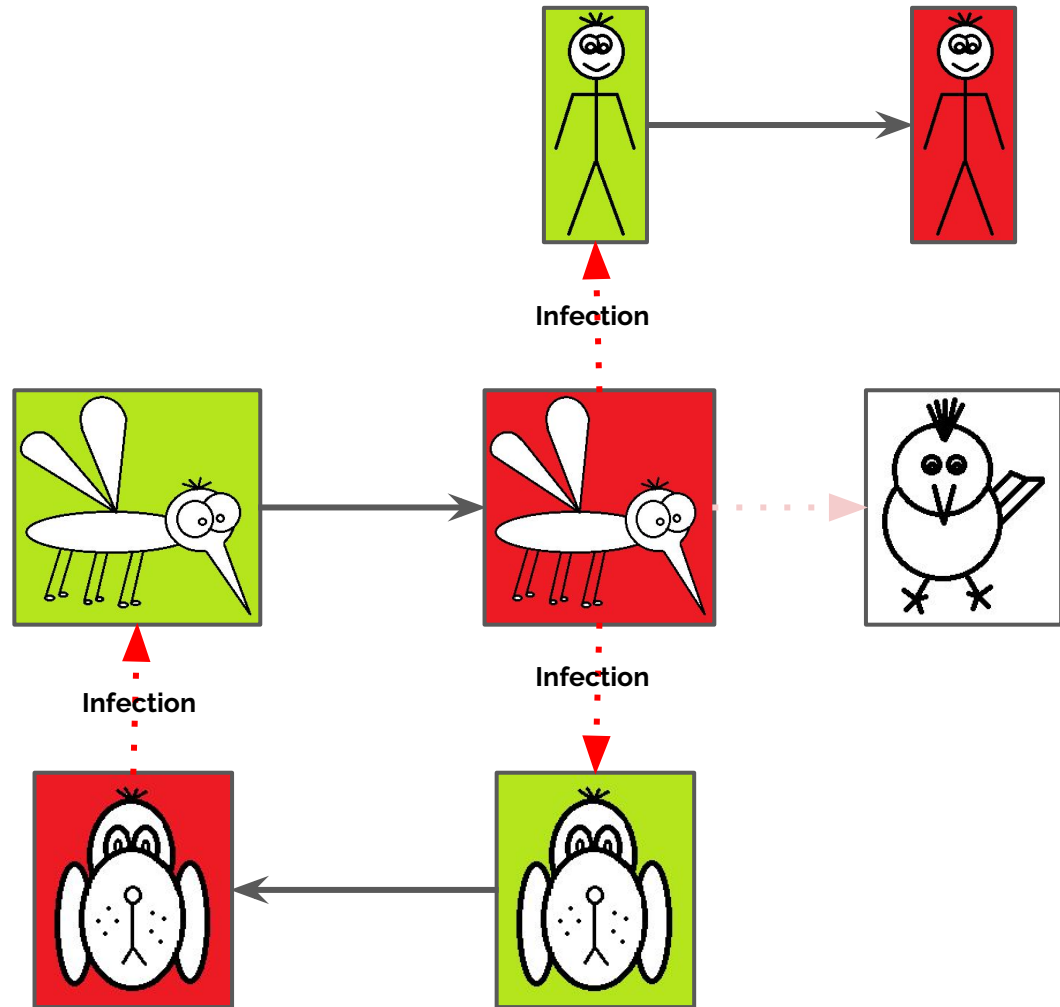
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- **Human infection** alone cannot maintain transmission.



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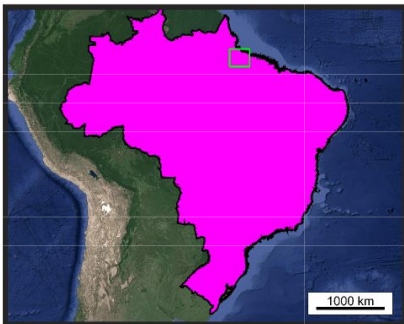
- A vector-borne disease spread by **sandflies**.
- In Brazil, **domestic dogs** are the main reservoir.
- **Human infection** alone cannot maintain transmission.
- Sandflies feed on other dead-end hosts: for example, **chickens**.



VL in Brazil

- VL is endemic in parts of Brazil.
- Serological studies have estimated **prevalence in dogs** to range between 25% and 50% in endemic northern regions.
- The number of **human cases has increased rapidly** in the last 30 years: 3,500 reported cases per year, 4,200 - 6,300 with underreporting.

Marajó island,
north Brazil.



Calderao village,
Marajo



Households
within Calderao



Previous VL models

Table 1. Summary of VL modelling papers

	Refs																								
	Anthroponotic studies								Zoonotic studies																
	[16]	[61]	[13]	[62]	[10] ^a	[17]	[12] ^a	[11] ^a	[63]	[57]	[40]	[64]	[65]	[41]	[58]	[66]	[67]	[42]	[28] ^b	[29] ^b	[14]	[15] ^b	[68]	[59]	
Model structure																									
Deterministic	✓ ^c		✓		✓		✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓		✓	✓	✓	
Host-only	✓	✓		✓		✓			✓		✓	✓	✓	✓	✓	✓									✓
Assumption																									
Asymptomatic humans					✓	✓	✓	✓																	
PKDL					✓	✓	✓	✓											✓	✓			✓		
Humans	✓	✓	✓	✓	✓	✓	✓	✓			†						†	†	✓	✓			✓	✓	
Asymptomatic dogs											✓														✓
Spatial aspects																									
Seasonality											✓		✓	✓					✓						
Intervention																									
Human treatment		✓	✓	✓	✓	✓	✓	✓											✓	✓			✓		
Human vaccination						✓					✓												✓		
Vector control					✓		✓				✓									✓				✓	
Dog culling															✓	✓	✓							✓	✓
Dog collar															✓									✓	✓
Dog treatment											✓										*			✓	✓
Dog vaccination											✓													✓	✓
Region	India	Sudan	India	ISC	ISC	India	India	ISC	France	–	–	Brazil/ Malta	–	Brazil	Brazil	Brazil	Brazil	Morocco	Sudan	–	France	–	Brazil	Brazil	

^aDenotes studies by Stauch *et al.* that use the same basic model.

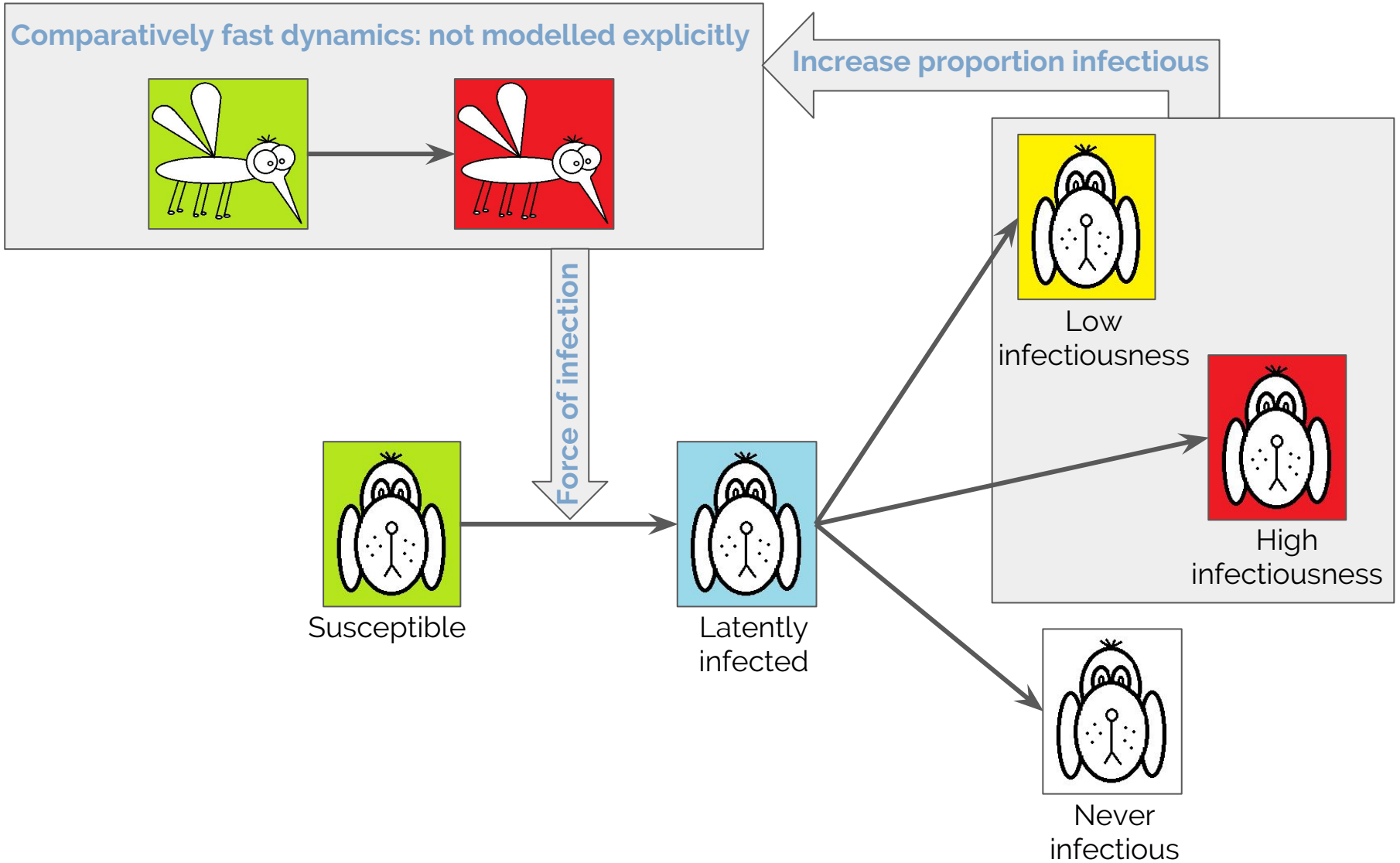
^bDenotes studies by Elmojtaba *et al.* that use the same basic model.

^c✓, included in model; †, dead-end hosts; *, implicitly included in other terms; –, unclear or unknown region.

Reference:

K.S.Rock et al (2015) Uniting mathematics and biology for control of visceral leishmaniasis. *Trends in Parasitology*, **31**(6):251-259..

Our spatial modelling framework



Force of infection breakdown

- **Probability of** susceptible dog at household h **becoming infected** on day t :

$$p_h(t) = 1 - e^{-\lambda_h(t)}$$

- **Force of infection** comprised five components:

$$\lambda_h(t) = \alpha \times \delta \times L_h(t) \times \eta_{h,\text{dog}}(t) \times \phi_h(t)$$

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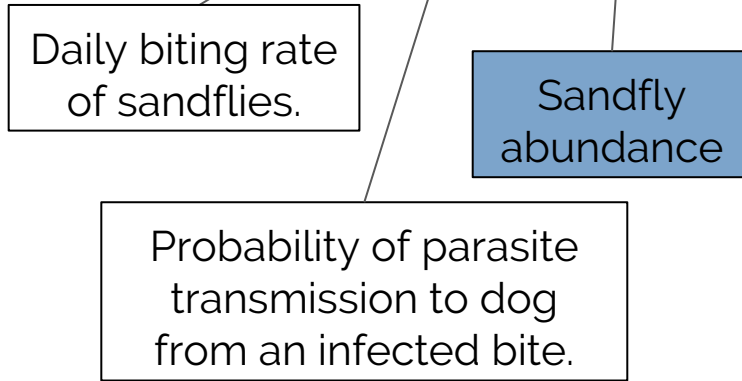
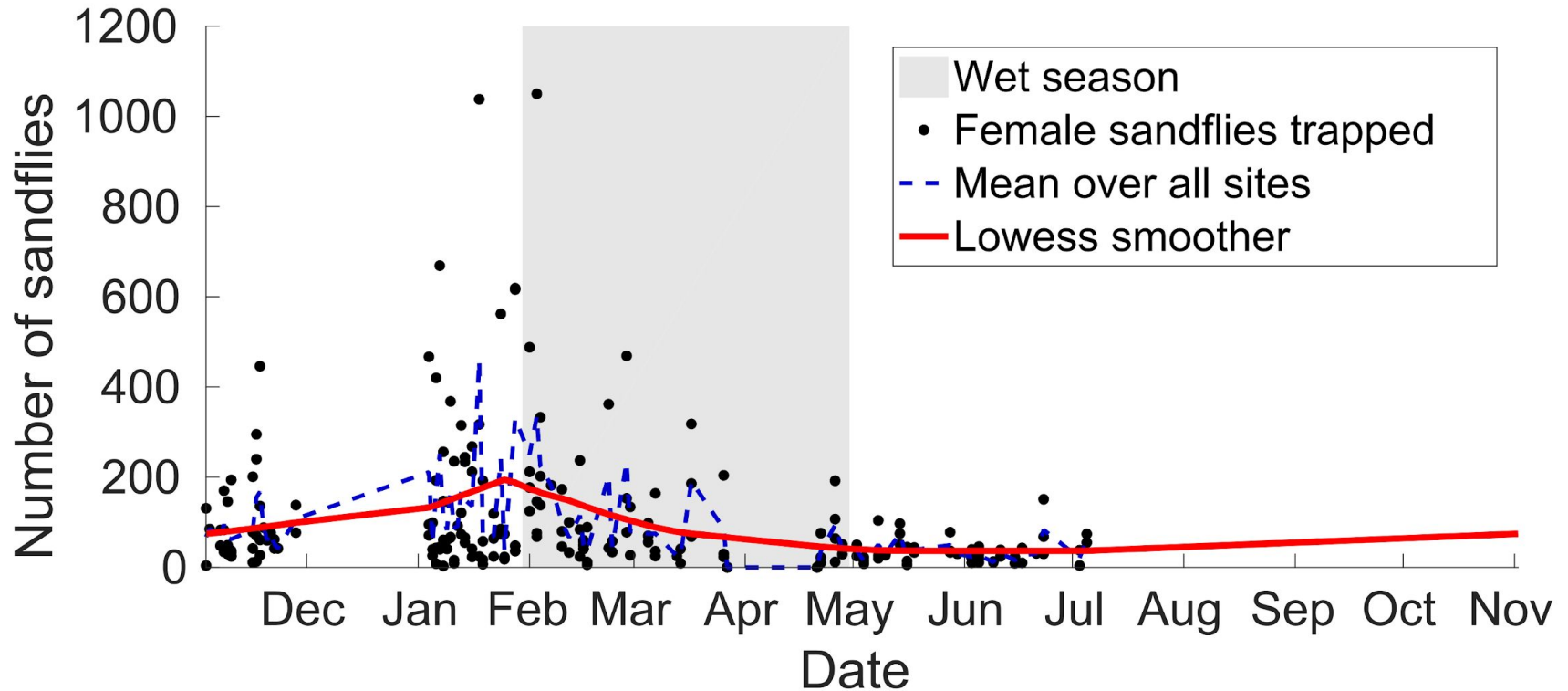


Figure 1: Seasonality of sandfly abundance



- **Peak in January**, at the transition from the dry to wet season.
- Minimum attained in May-June.

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Daily biting rate of sandflies.

Sandfly abundance

Probability of parasite transmission to dog from an infected bite.

Host preference towards dogs

Figure 2: Distributions of the number of hosts per household. Empirical data (bars), best fit Poisson distributions (blue, solid line) and negative binomial distributions (red, dashed line)

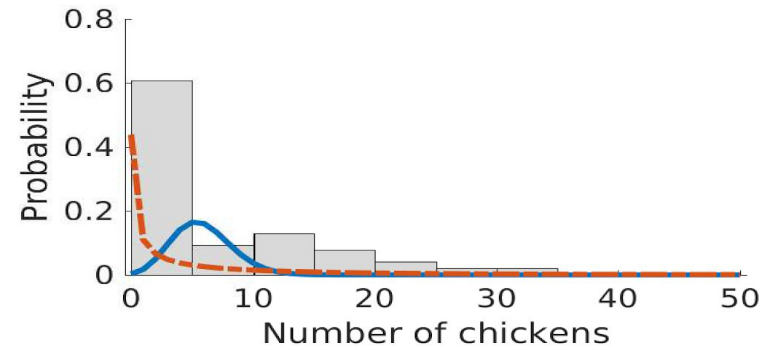
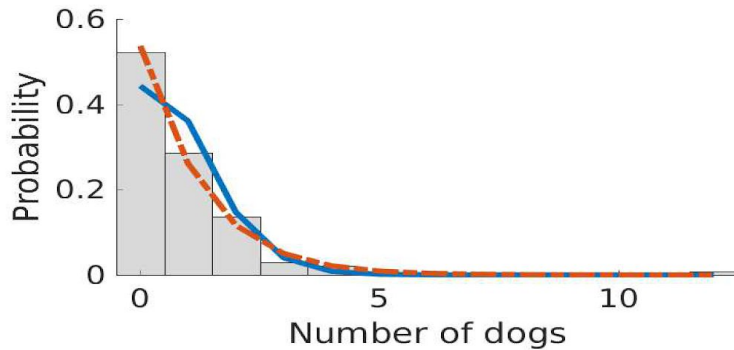
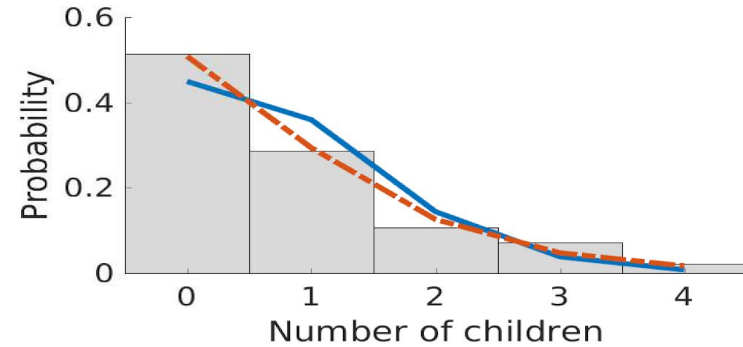
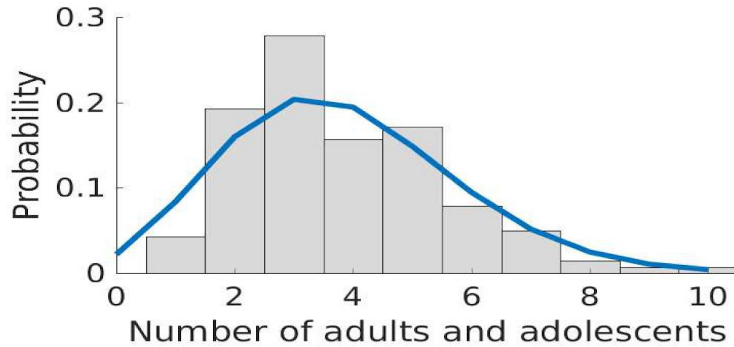
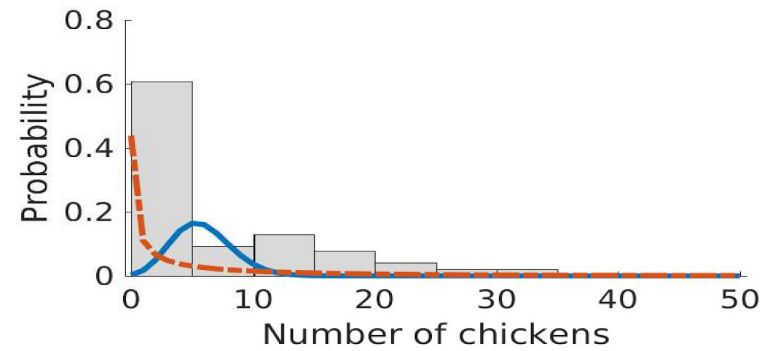
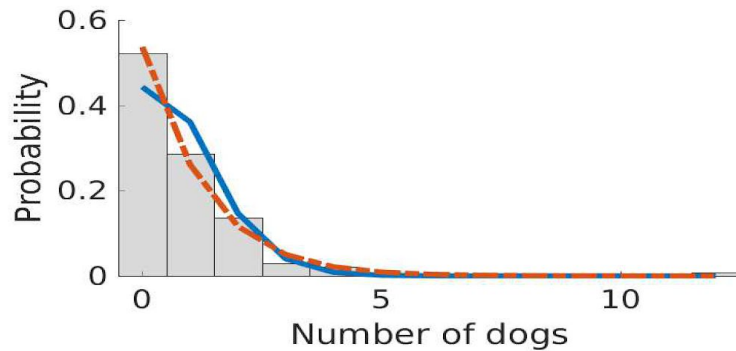
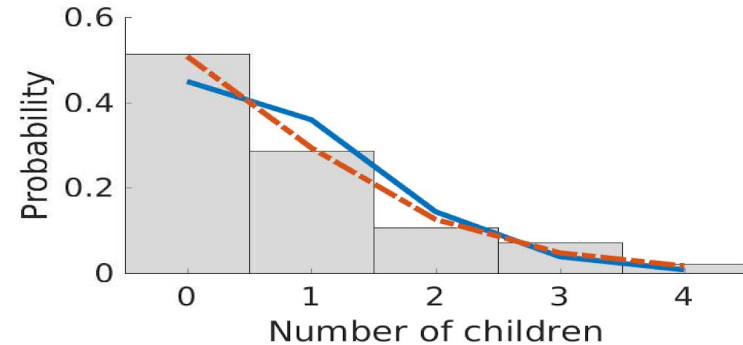
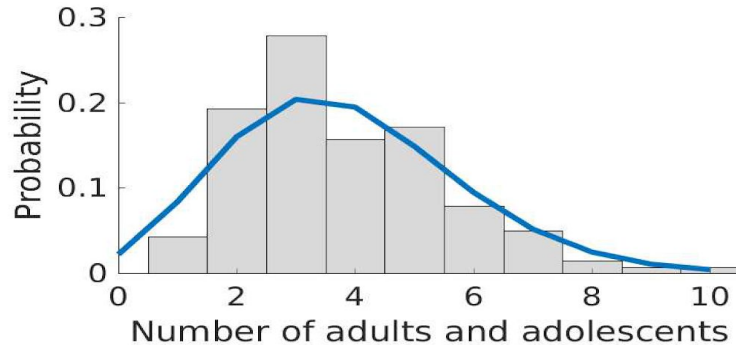


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- Sandfly biting preference towards host of interest drew on field and laboratory experiments.

Reference: R.J. Quinzel et al (1992) Host preferences of the phlebotomine sandfly *Lutzomyia longipalpis* in Amazonian Brazil. *Med. Vet. Entomol*, **6**(3):195-200.

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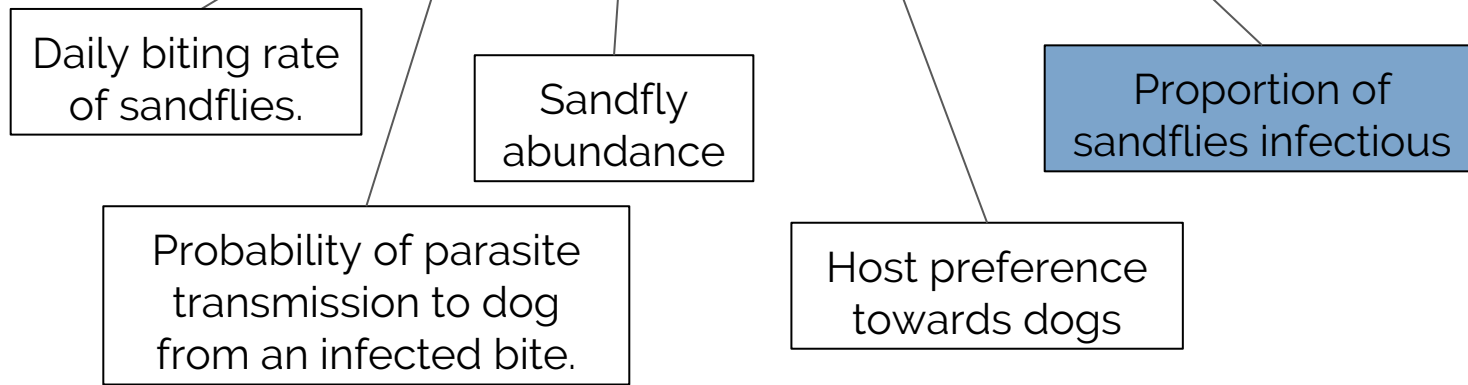
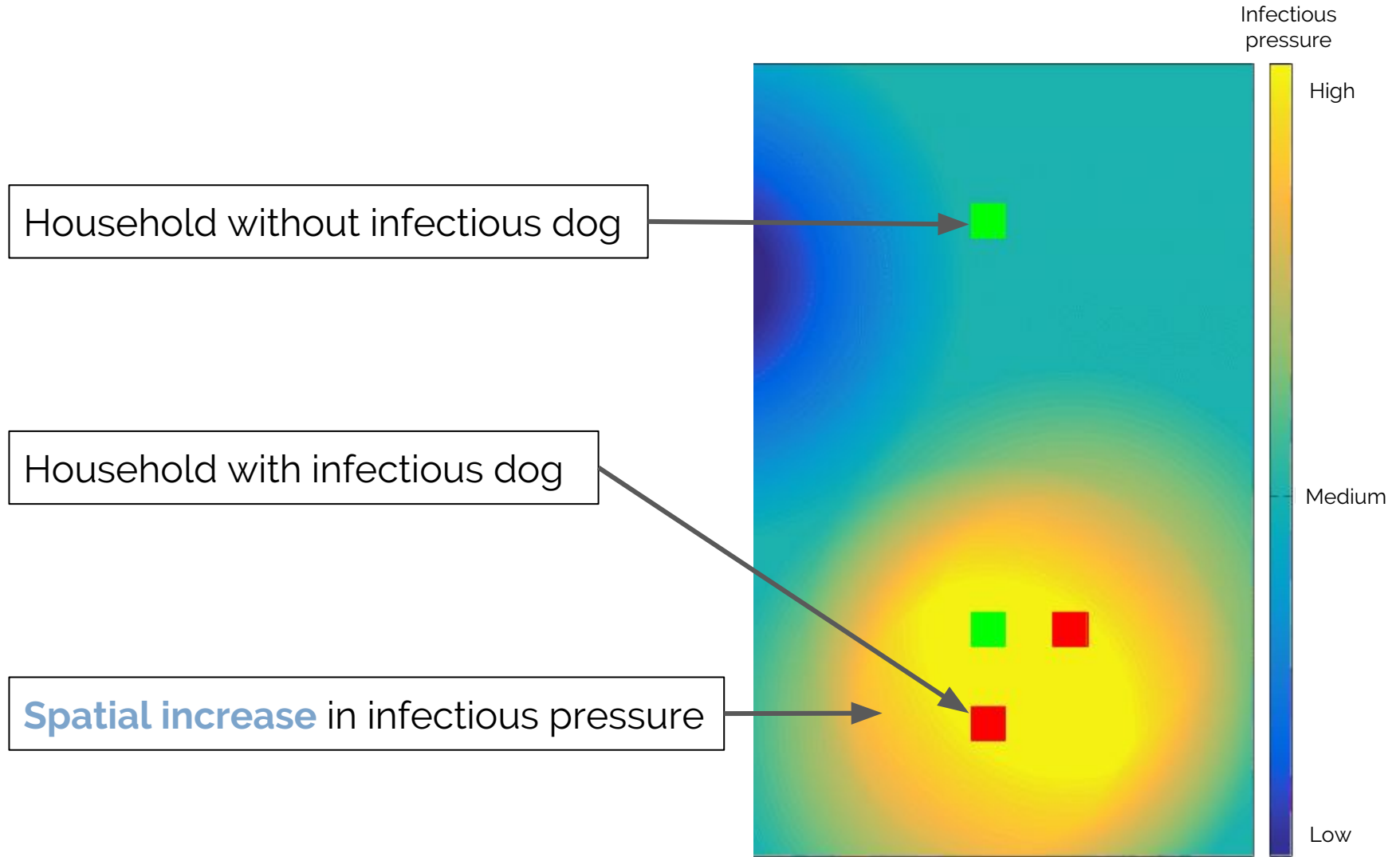


Figure 3: Spatial impact of infectious dogs on force of infection



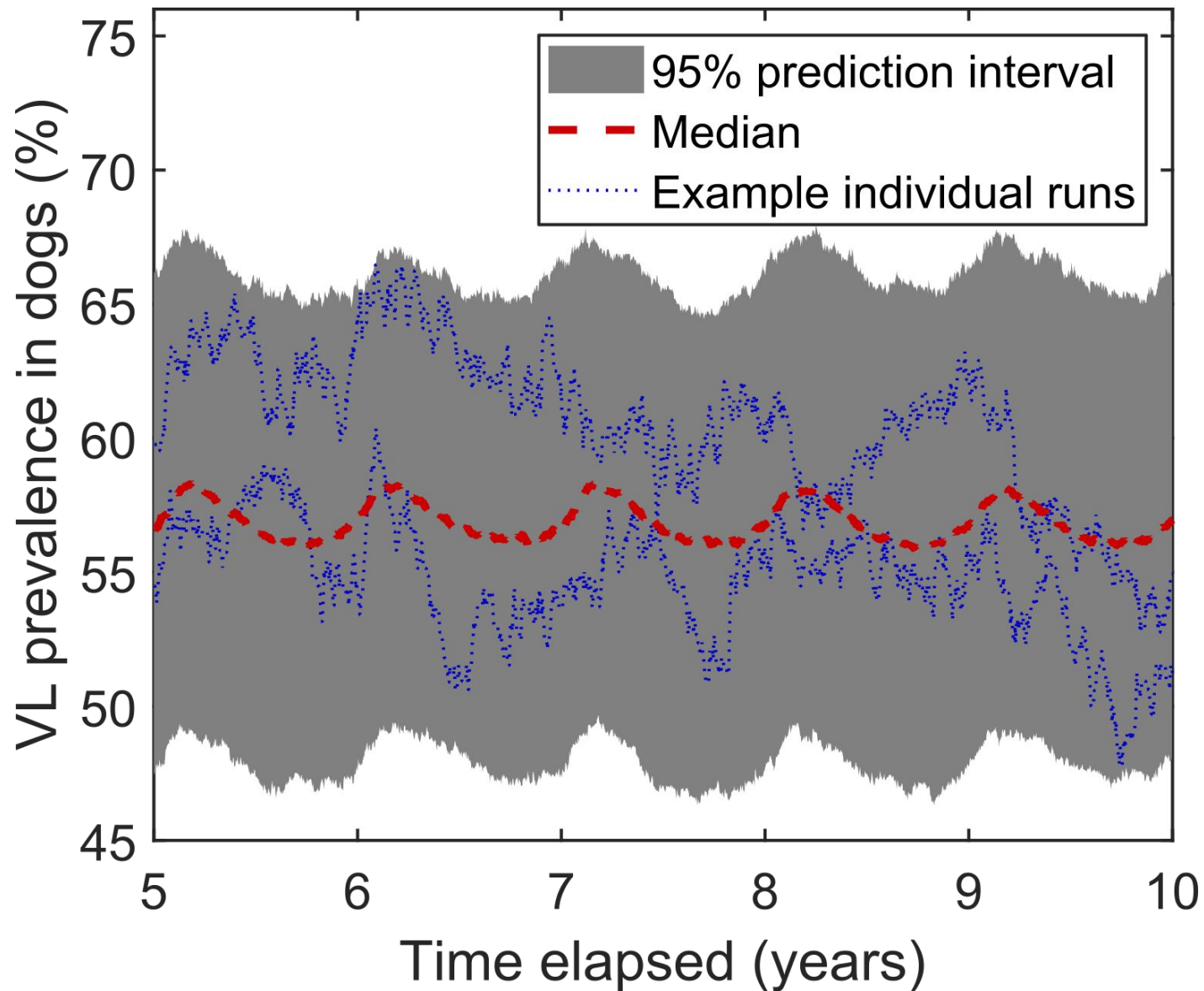
Model simulations

- Used spatial configuration of households in Calderao village.
- Force of infection used to compute probability of each susceptible dog becoming infected on current day.
- We keep track of the number of infected dogs each day: model output was **prevalence**.
- Outcomes were averaged over 1000 separate model runs.

Households within Calderao



Figure 4: Simulated VL prevalence in domestic dogs



Sensitivity Analysis

Parameter ID	Symbol	Description	Baseline value	Other values tested
1	r	Interaction range of sandflies (km).	0.30	0.02, 0.7, 2
2	π_{never}	Proportion of infected dogs that are never infectious.	0.55	0.14, 0.28, 0.42
3	$\tilde{\pi}_{\text{high}}$	Proportion of infectious dogs that are highly infectious.	0.37	0.25, 0.60, 0.80
4	ξ	Probability of a newly introduced dog being infected.	0.130	0.0064, 0.29, 0.43
5	ν	Per capita rate of progression of dogs from latently infected to a further state (Days^{-1}). $1/\nu$ is the average duration of the latent period (Days).	0.0055	0.0042, 0.0047, 0.0065
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- **Measure:** Average prevalence

$$\text{Average VL prevalence} = \frac{\sum_{t=T-364}^T \text{VL prevalence}(t)}{365}$$

- Performed a **one-at-a-time** sensitivity analysis.

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Analysed by: ⋮

- violin plots
- computing stochastic sensitivity coefficients

Reference:

Damiani et al (2013) Parameter sensitivity analysis of stochastic models: Application to catalytic reaction networks. *Computational biology and chemistry* **42**: 5-17.

Figure 5A: Violin plots for average VL prevalence

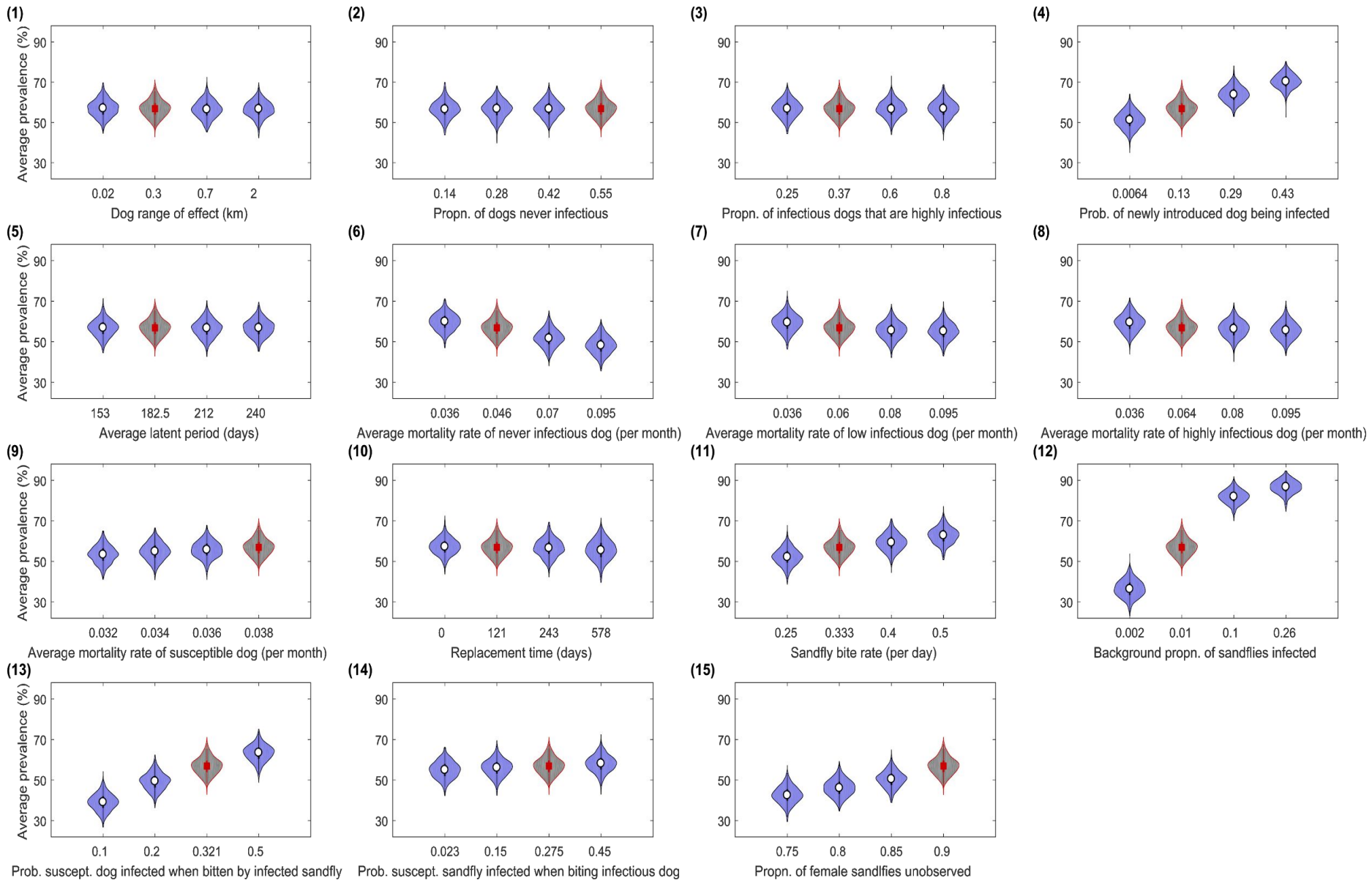


Figure 5A: Violin plots for average VL prevalence

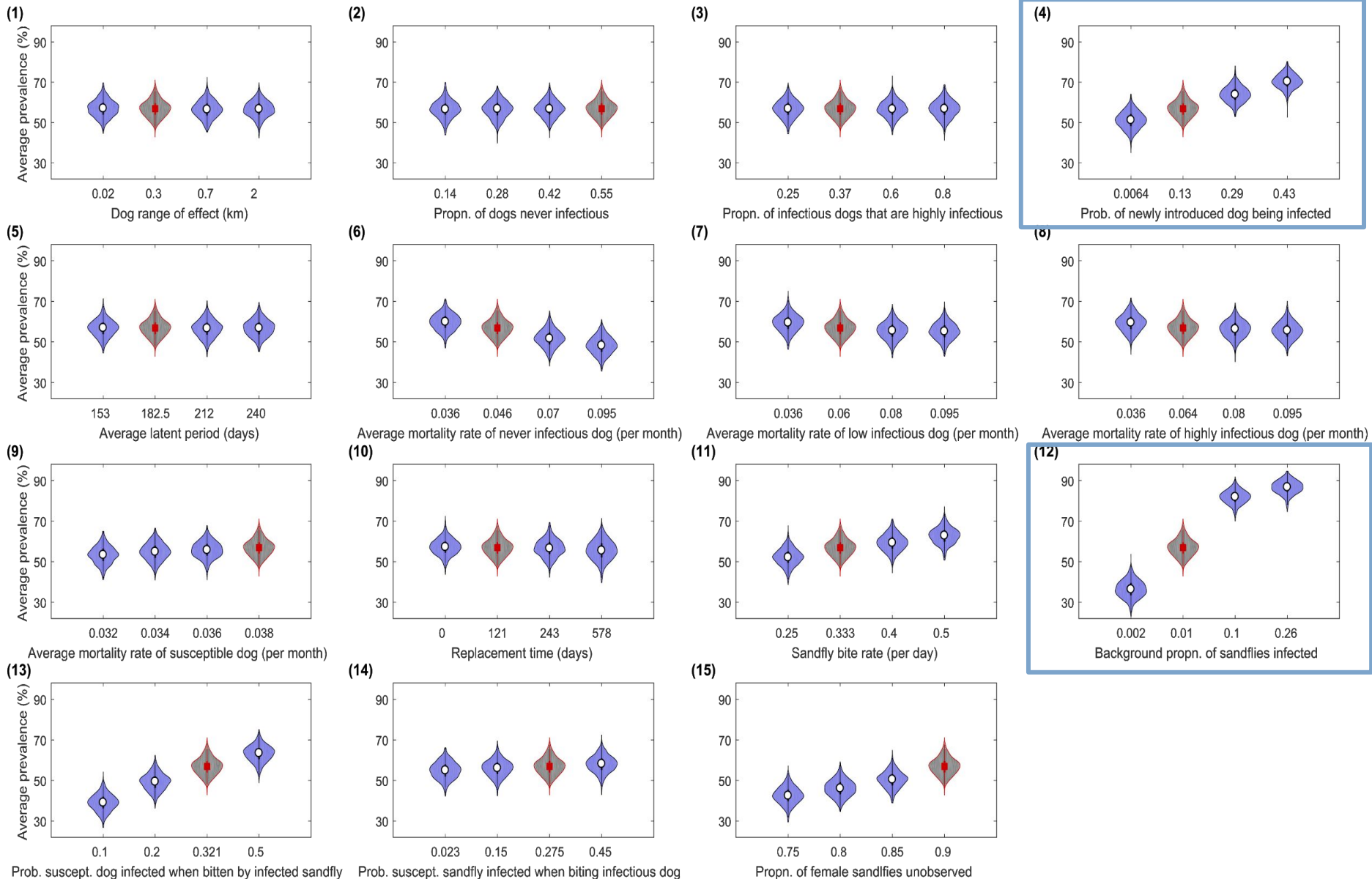


Figure 5B: Violin plots for average VL prevalence.

(Left) Background proportion of infected sandflies

(Right) Probability of a newly introduced dog being infected

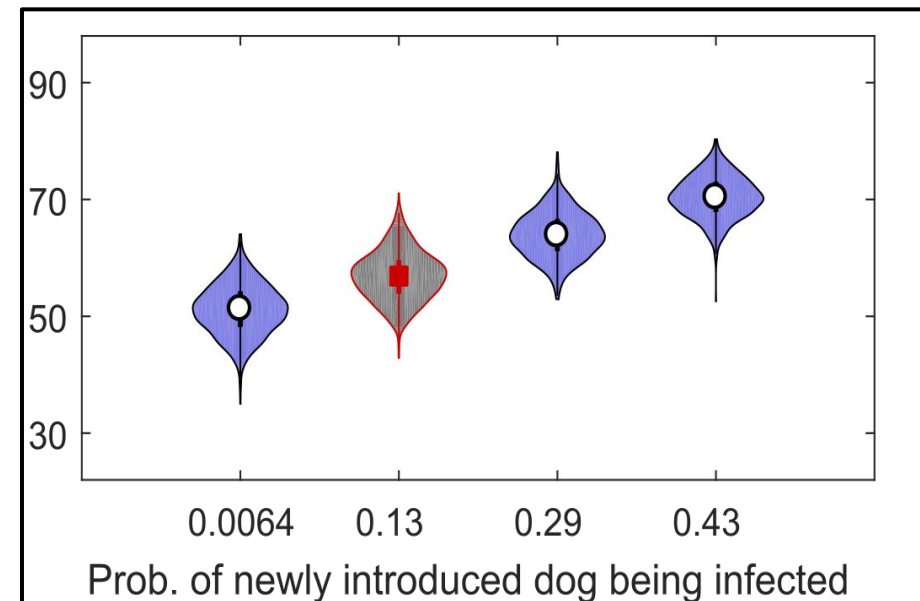
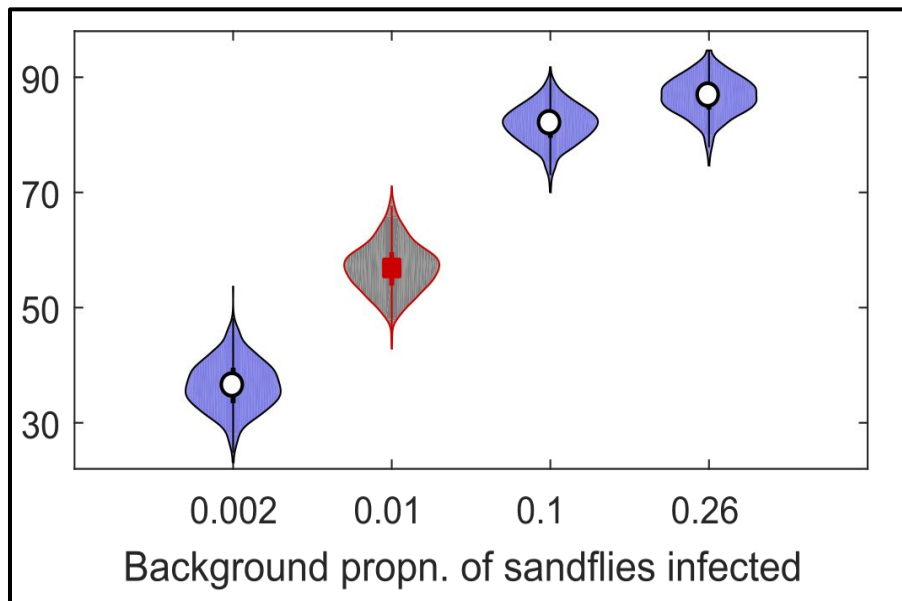


Figure 6: Stochastic sensitivity coefficient parameter ranking

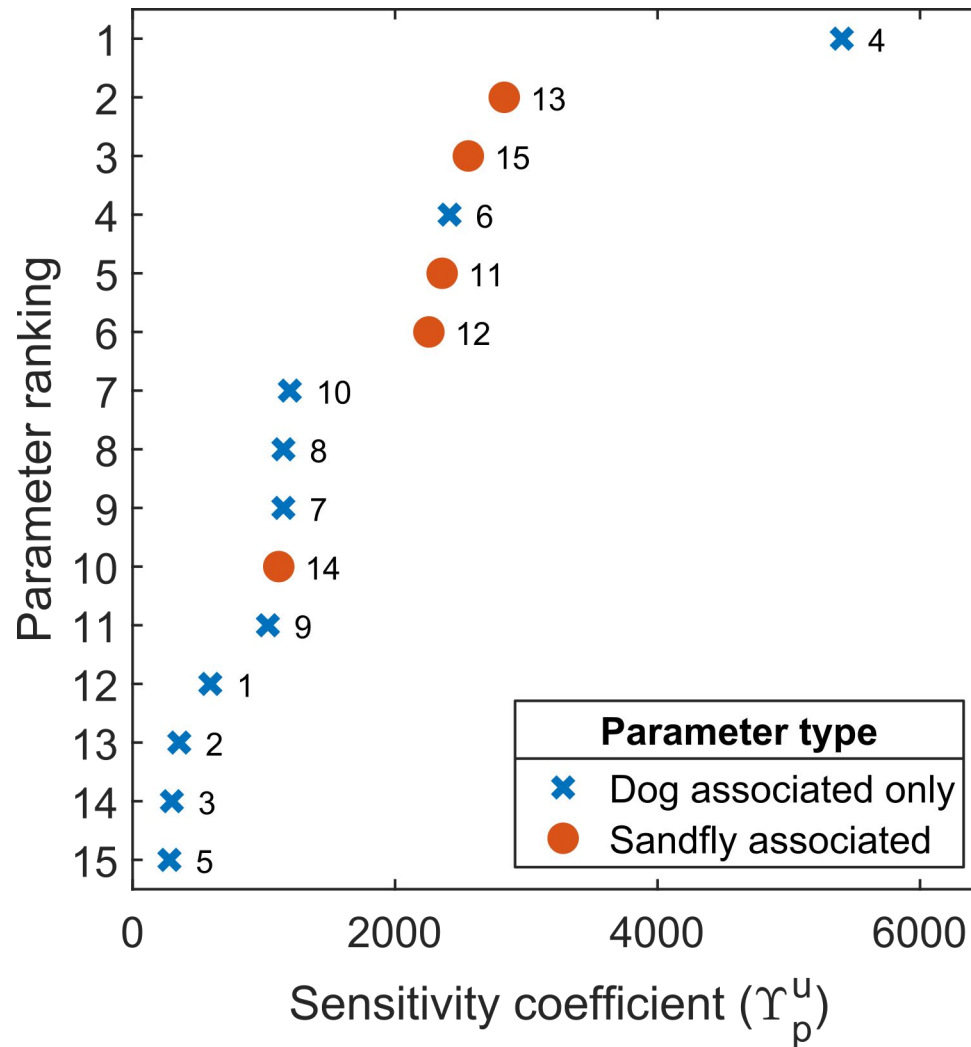
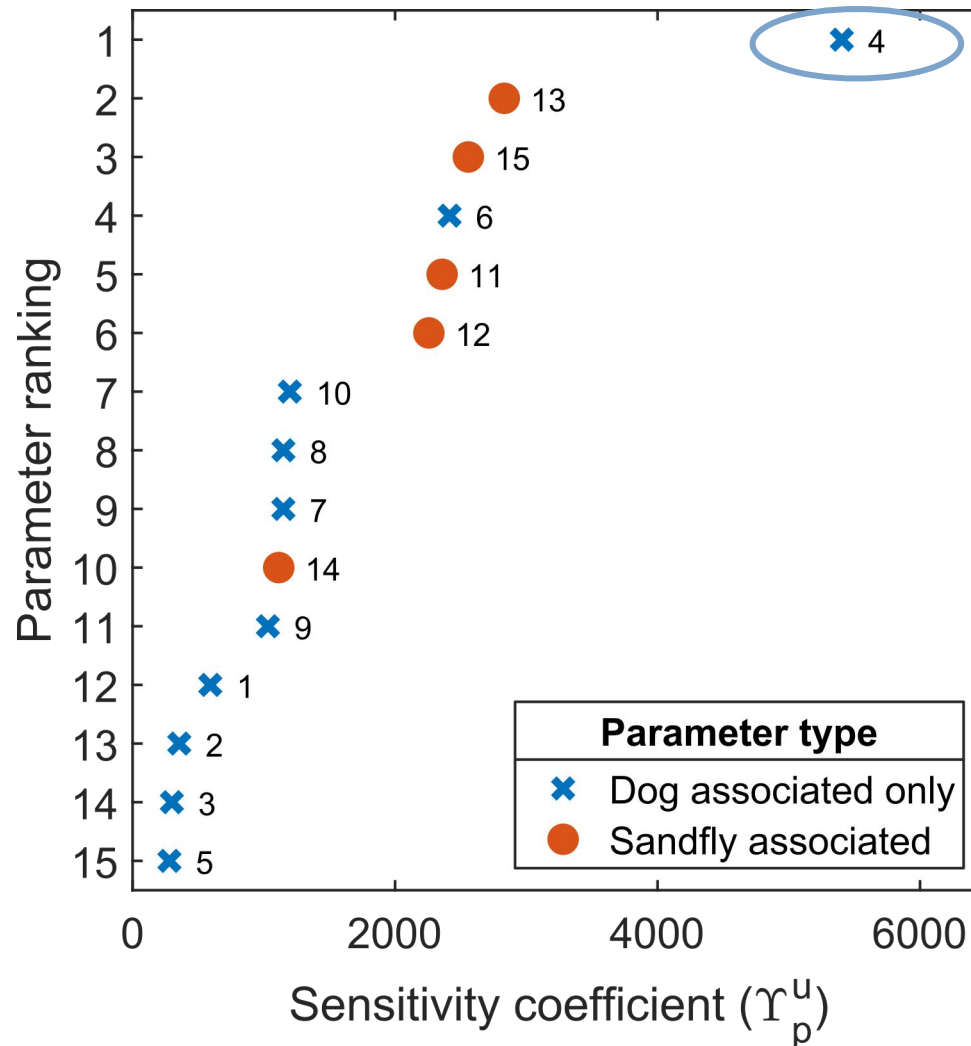
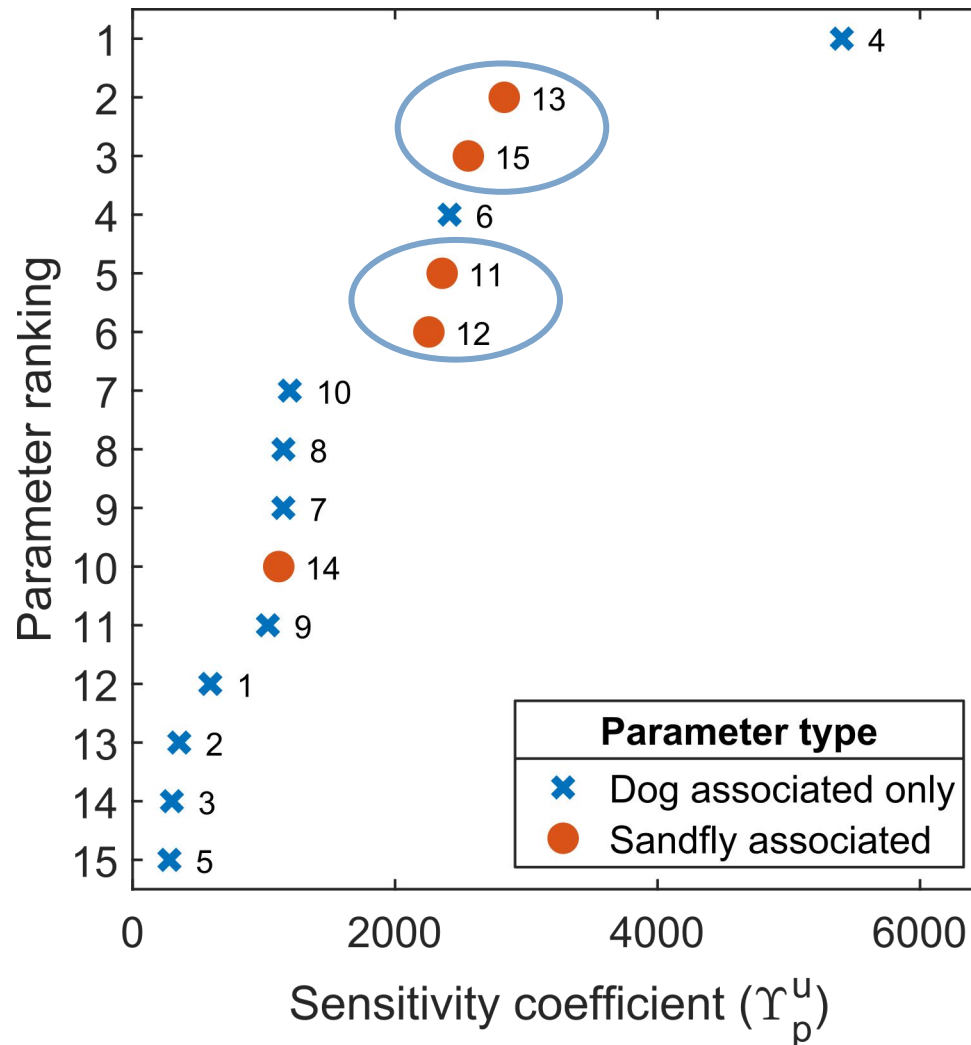


Figure 6: Stochastic sensitivity coefficient parameter ranking



- Average VL disease prevalence was most sensitive to the probability of a newly introduced dog being infected.

Figure 6: Stochastic sensitivity coefficient parameter ranking



- Four parameters associated with sandflies were among the top six ranked parameters.

Conclusions and next steps

- Developed a novel individual-based, spatio-temporal mechanistic modelling framework for VL in dogs.
- Sensitivity analysis motivates future data collection efforts.
- Provides a platform to stimulate the formulation of innovative mathematical models into:
 - spatial spread of zoonotic VL infection in humans
 - intervention planning

Thank you, questions?

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